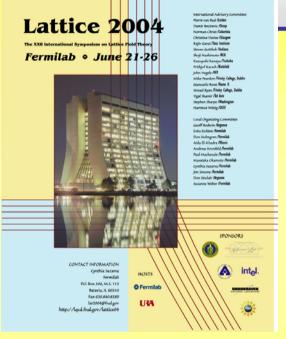
THE ROLE OF LATTICE QCD IN FLAVOR PHYSICS



see also talks by:
M.Wingate (LQCD)
I.Shipsey (Exp.)

Vittorio Lubicz





OUTLINE

- 1. Flavor physics and its motivations
- 2. First row unitarity and the Cabibbo angle
- 3. The unitarity triangle analysis
- 4. New Physics

Special thanks to P.Gambino, L.Giusti, G.Isidori, S.Sharpe, and all the members of the UTfit Collaboration

1

FLAVOR PHYSICS AND ITS MOTIVATIONS

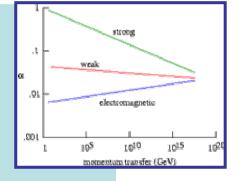
THE STANDARD MODEL: A LOW ENERGY EFFECTIVE THEORY

CONCEPTUAL PROBLEMS The most obvious:

o Gravity: $M_{Planck} = (\hbar c/G_N)^{1/2} \approx 10^{19} \text{ GeV}$

PHENOMENOLOGICAL INDICATIONS

- o Unification of couplings ($M_{GUT} \approx 10^{15}-10^{16}$ GeV)
- o Dark matter ($\Omega_{\rm M} \approx 0.35$)
- o Neutrino masses



- o Matter/Anti-matter asymmetry (not enough & in the SM)
- o Cosmological vacuum energy

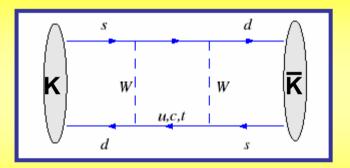
THE "NATURAL" CUT-OFF:

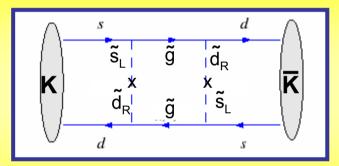
NEW PHYSICS MUST BE VERY "SPECIAL"

$$\delta m_{\rm H}^2 = \frac{3G_{\rm F}}{\sqrt{2\pi}^2} m_{\rm t}^2 \Lambda^2 \approx (0.3 \ \Lambda)^2 \longrightarrow \Lambda = O(1 \ {\rm TeV})$$

MOTIVATIONS FOR FLAVOR PHYSICS

- We do not understand flavor physics: Why 3 families? Why the hierarchy of masses?
- We expect New Physics effects in the flavor sector:





THE FLAVOR PROBLEM: Ako_ko ≈ O(100 TeV)

- 10 parameters in the quark sector (6 m_q + 4 CKM)
- Is the CKM mechanism and its explanation of \mathcal{L}^{p} correct?

PRECISION ERA OF FLAVOR PHYSICS

$$\varepsilon_{\rm K} = (2.271 \pm 0.017) \times 10^{-3}$$
 0.7%

$$\Delta m_d = (0.503 \pm 0.006) \text{ ps}^{-1}$$
 1%

$$\sin(2\beta) = 0.734 \pm 0.054$$
 7%

.

EXPERIMENTS

We need to control the theoretical input parameters at a comparable level of accuracy!!

2

FIRST ROW UNITARITY AND THE CABIBBO ANGLE

$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$ The most stringent unitarity test

SFT:
$$|V_{ud}| = 0.9740 \pm 0.0005$$
 Extremely precise, 9 expts N β -dec: $|V_{ud}| = 0.9731 \pm 0.0015$ g_V/g_A , will be improved at PERKEO, Heidelb. π_{e3} : $|V_{ud}| = 0.9765 \pm 0.0056$ Theor. clean, but BR=10-8 PIBETA at PSI

Average: $|V_{ud}| = 0.9739 \pm 0.0005$ G. Isidori et al., CKM 2002 Workshop

PDG 2002 average

$$b \rightarrow u$$
 $|V_{ub}| = 0.0036 \pm 0.0007$ $|V_{ub}|^2 \approx 10^{-5}$

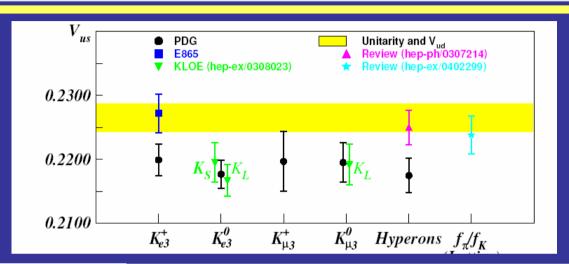
 $K \rightarrow \pi ev$: $|V_{us}| = 0.2196 \pm 0.0026$

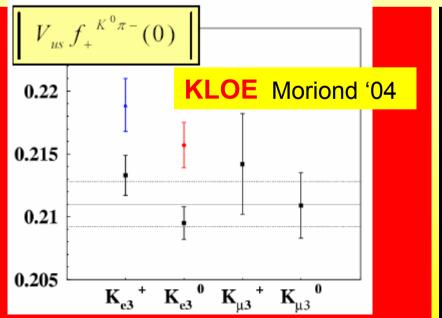
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = -0.0042 \pm 0.0019$$

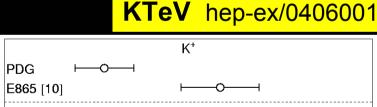
The NEW experimental results

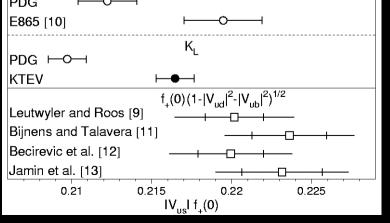


PRL 91, 261802 (and Moriond '04)









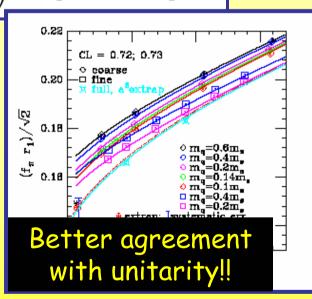
Theory: 2 recent lattice contributions

1) LEPTONIC DECAYS:

$$\frac{\Gamma(K \to \mu \bar{\nu}_{\mu}(\gamma))}{\Gamma(\pi \to \mu \bar{\nu}_{\mu}(\gamma))} \ = \left(\frac{|V_{us}|^2 f_K^2 m_K \left(1 - \frac{m_{\mu}^2}{m_K^2}\right)^2}{|V_{ud}|^2 f_{\pi}^2 m_{\pi} \left(1 - \frac{m_{\mu}^2}{m_{\pi}^2}\right)^2} \ 0.9930(35) \right)$$
[Rad.Corr.]

Precise f_K/f_{π} , MILC Latt.'03-04 Asqtad action, $N_f=3$

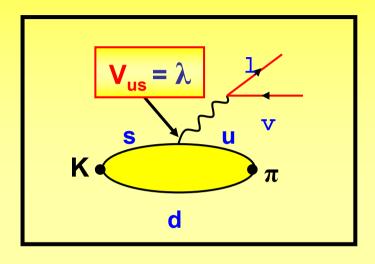
$$f_{\pi} = 129.5 \pm 0.9_{\text{stat}} \pm 3.6_{\text{syst}} \text{ MeV}$$
 $f_{K} = 156.6 \pm 1.0_{\text{stat}} \pm 3.8_{\text{syst}} \text{ MeV}$
 $f_{K}/f_{\pi} = 1.210 \pm 0.004_{\text{stat}} \pm 0.013_{\text{syst}}$



C. Bernard, update of Marciano 2004: $|V_{us}| = 0.2219(26)$

2) SEMILEPTONIC KI3 DECAYS:

Precise (quenched) calculation of f(0), SPQcdR 2004



$$\Gamma_{\text{K13}} = C^1 \frac{G_F^2 |V_{\text{us}}|^2 M_K^5}{192 \pi^3} S_{\text{EW}} (1+\delta_K^1) I_K^1 f_+(0)^2$$

The largest th. uncertainty from:

$$f_{+}(0) = 1 - O(m_s - m_u)^2$$

[Ademollo-Gatto theorem]

ChPT

$$f_{+}(0) = 1 + f_{2} + f_{4} + O(p^{8})$$



"Standard" estimate:
Leutwyler, Roos (1984)
(QUARK MODEL) $f_4 = -0.016 \pm 0.008$

Vector Current Conservation

f₂ = - 0.023 Independent of L_i (Ademollo-Gatto)

THE LARGEST UNCERTAINTY

ChPT: The complete O(p⁶) calculation

Post, Schilcher (2001), Bijnens, Talavera (2003)

$$f_4 = \Delta_{loops}(\mu) - \frac{8}{F_{\pi}^4} [C_{12}(\mu) + C_{34}(\mu)] (M_K^2 - M_{\pi}^2)^2$$

 C_{12} (μ) and C_{34} (μ) can be determined from the slope and the curvature of the scalar form factor. Experimental data, however, are not accurate enough.

... and models

```
Jamin et al., f_4^{LOC} = -0.018 ± 0.009 [Coupled channel dispersive analysis] Cirigliano et al., f_4^{LOC} = -0.012 [Resonance saturation] Cirigliano et al., f_4^{LOC} = -0.016 ± 0.008 [QM, Leutwyler and Roos]
```

$$\mu = ??? \Delta_{loops}(1GeV) = 0.004 \Delta_{loops}(M_{\rho}) = 0.015 \Delta_{loops}(M_{\eta}) = 0.031$$

Cirigliano et al.,
$$f_{+}^{K^0\pi^-}(0) = 0.981 \pm 0.010$$

The Lattice QCD calculation

Talk by F. Mescia (and hep-ph/0403217)

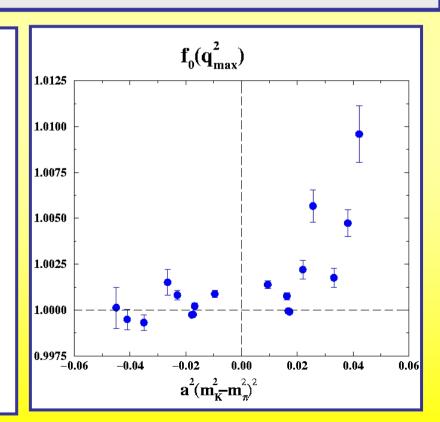
1) Evaluation of $f_0(q_{MAX}^2)$

The basic ingredient is a double ratio of correlation functions:

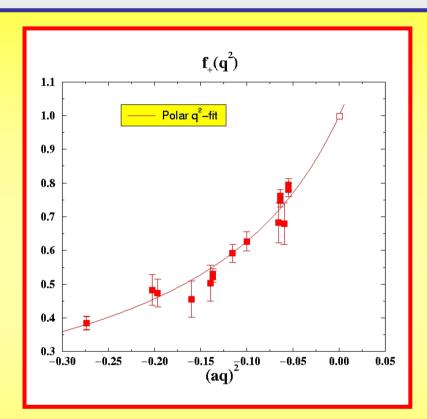
$$R = \frac{\langle \pi | \bar{s} \gamma_0 u | K \rangle \langle K | \bar{u} \gamma_0 s | \pi \rangle}{\langle \pi | \bar{u} \gamma_0 u | \pi \rangle \langle K | \bar{s} \gamma_0 s | K \rangle}$$

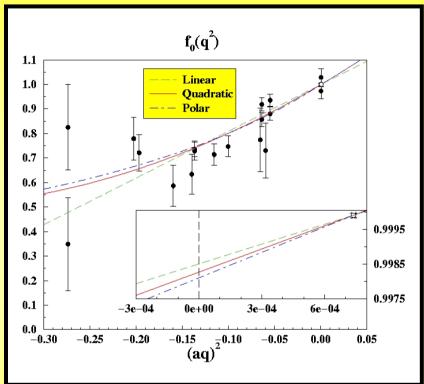
$$= \frac{(M_K + M_\pi)^2}{4M_K M_\pi} f_0(q_{max}^2)^2$$

[FNAL for B->D*]



Extrapolation of $f_0(q_{MAX}^2)$ to $f_0(0)$





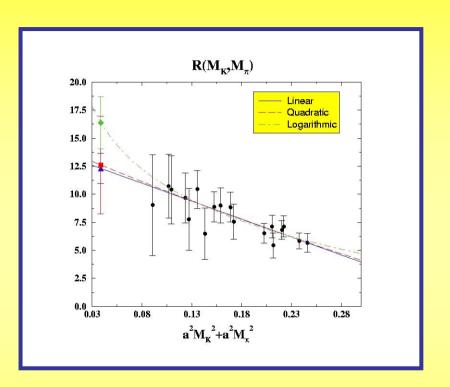
Comparison of polar fits:

 $\lambda_{+} = (25 \pm 2) 10^{-3}$ LQCD:

 $\lambda_0 = (12 \pm 2) \cdot 10^{-3}$

 $\lambda_{+} = (24.11 \pm 0.36) 10^{-3}$ $\lambda_{0} = (13.62 \pm 0.73) 10^{-3}$ KTeV:

3) Chiral extrapolation



$$R = \frac{f_{+}(0)-1-f_{2}^{QUEN}}{(M_{K}^{2}-M_{\pi}^{2})^{2}}$$

Computed in Quenched-ChPT

The dominant contributions to the systematic error come from the uncertainties on the q² and mass dependencies of the form factor

$$f_{+}^{K^0\pi^-}(0) = 0.960 \pm 0.005_{stat} \pm 0.007_{syst}$$

[Quenching error is not included]

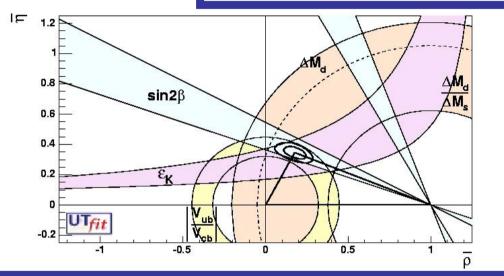
In agreement with LR!!



THE UNITARITY TRIANGLE ANALYSIS

THE UNITARITY TRIANGLE ANALYSIS





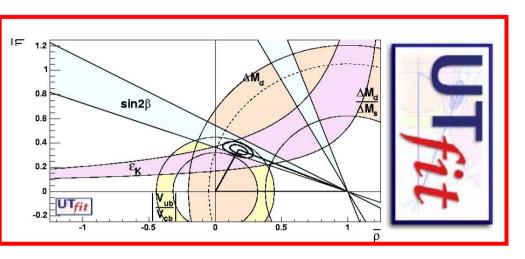
5 CONSTRAINTS2 PARAMETERS

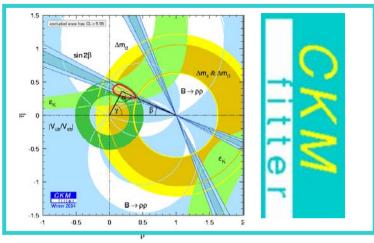
Hadronic Matrix Elements from LATTICE QCD

(b→u)/(b→c)	$\bar{\rho}^2 + \bar{\eta}^2$	f ₊ ,F(1),
ε _K	$\frac{1}{\eta}[(1-\overline{\rho})+P]$	B _K
$\Delta m_{\sf d}$	$(1-\bar{\rho})^2 + \bar{\eta}^2$	f _{Bd} B _{Bd}
$\Delta m_d / \Delta m_s$	$(1-\bar{\rho})^2 + \bar{\eta}^2$	ξ
A(J/ψ K _s)	$sin2\beta(\overline{\rho},\overline{\eta})$	



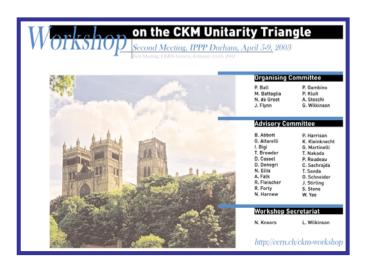
Bayesian and frequentist: 2 stat. approaches





and 2 dedicated workshop





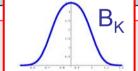
The Bayesian approach

The Bayes Theorem: $P(A/B) \sim P(B/A) P(A)$

$$f(\bar{p}, \bar{\eta}, \mathbf{x} | c_1, ..., c_m) \sim \prod_{j=1,m} f_j(\mathbf{c} | \bar{p}, \bar{\eta}, \mathbf{x}) \prod_{i=1,N} f_i(\mathbf{x}_i) f_o(\bar{p}, \bar{\eta})$$
Integrat. over \mathbf{x}

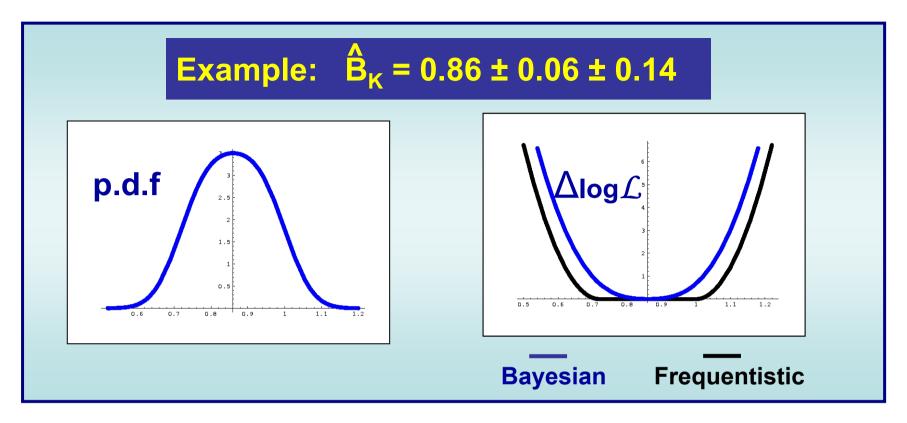
$$f(\bar{p}, \bar{\eta} | \mathbf{c}) \sim \mathcal{L}(\mathbf{c} | \bar{p}, \bar{\eta}) f_o(\bar{p}, \bar{\eta})$$

The p.d.f. $f(x_i)$ represents our "degree of beliefs"



The Frequentistic approach

The theoretical likelihood do not contribute to the χ^2 of the fit while the corresponding parameters take values within the "allowed" ranges. Instances where even only one of the parameters trespasses its range are not considered.



In the frequentistic approach the selected region does not have a precise statistical meaning ("at least 95%"). Nevertheless, if same likelihood are used, the output results are very similar

Estimates of the uncertainties for lattice determinations should be given by the lattice community

Unitary Triangle Analysis: LQCD INPUT PARAMETERS

$K - \overline{K}$ mixing and B_K

Stat., Match.

Quench., Chiral

 \hat{B}_{K} = 0.86 ± 0.06 ± 0.14

 $A = 0.87 \pm 0.06 \pm 0.13$

LATT03 average: D. Becirevic

Error:

7%

16%

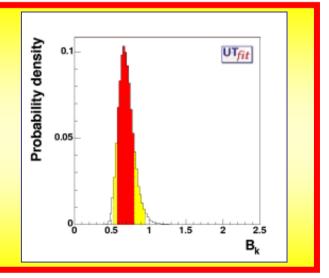
Projected:

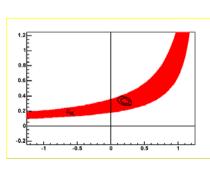
7%

Error from other sources ≈ 10% (mainly V_{cb})

From the UT fit

$$\hat{B}_{K}$$
= 0.65 ± 0.10 15%





$B_{B_{d/s}} - \overline{B}_{B_{d/s}}$ mixing: $f_{B_s} \sqrt{B_{B_s}}$ and ξ (I)

Stat & Syst

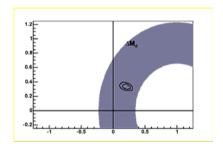
$$f_{Bs}\sqrt{B_{Bs}} = 276 \pm 38 \text{ MeV}$$

Error: 14%

Projected: 5%

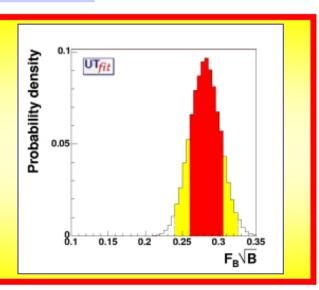
 $f_{Bs}\sqrt{B_{Bs}}$ = 270 ± 40 MeV

LATT03 average: A. Kronfeld



From the UT fit

$$f_{Bs}\sqrt{B_{Bs}} = 279 \pm 21 \text{ MeV}$$



$B_{B_{d/s}} - \overline{B}_{B_{d/s}}$ mixing: $f_{B_s} \sqrt{B_{B_s}}$ and ξ (II)

Stat.

Syst.

$$\xi = 1.24 \pm 0.04 \pm 0.06$$

 $\xi = 1.25 \pm 0.10$

LATT03 average: A. Kronfeld

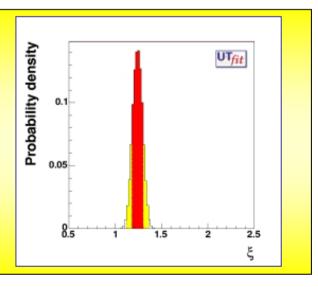
Error: 3% 5%

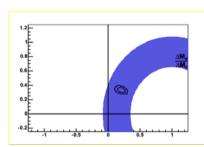
Projected: 3%

From the UT fit

$$\xi = 1.22 \pm 0.05$$

4%





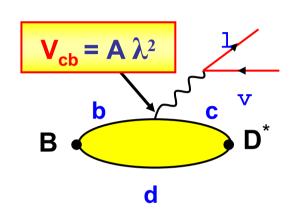
V_{cb} from exclusive semil. B-decays

Exp. Theor.

$$V_{cb}^{Excl.} = (42.1 \pm 1.1 \pm 1.9) \cdot 10^{-3}$$

Error: 2.6% 4.5%

Projected: ??



$$F_{B\to D^*}(1) = 0.91 \pm 0.04$$

Mainly from LQCD, FNAL Compatible with QCDSR and HQET

+ Quark Model

$$V_{cb}^{Incl.} = (41.4 \pm 0.7 \pm 0.6) \cdot 10^{-3}$$

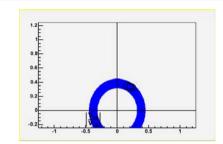
Dominant contribution to the average

$$V_{cb}^{Aver.} = (41.5 \pm 0.7) \cdot 10^{-3}$$

V_{ub} from exclusive semil. B-decays

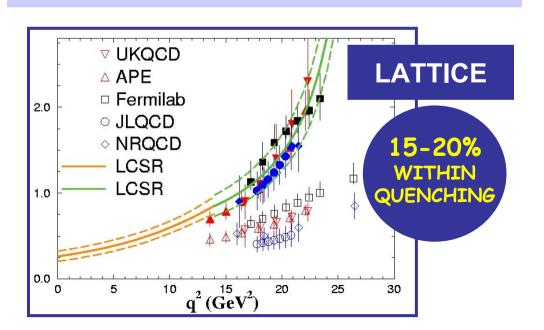
Exp. Theor.

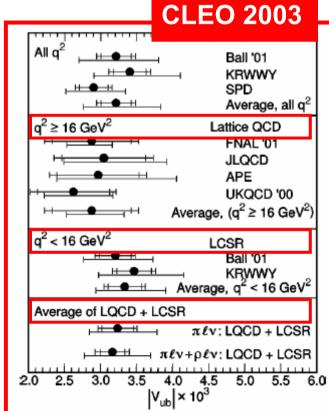
$$V_{ub}^{Excl.} = (32.4 \pm 2.4 \pm 4.6) \cdot 10^{-4}$$



Error: 7% 14%

Projected: 7%



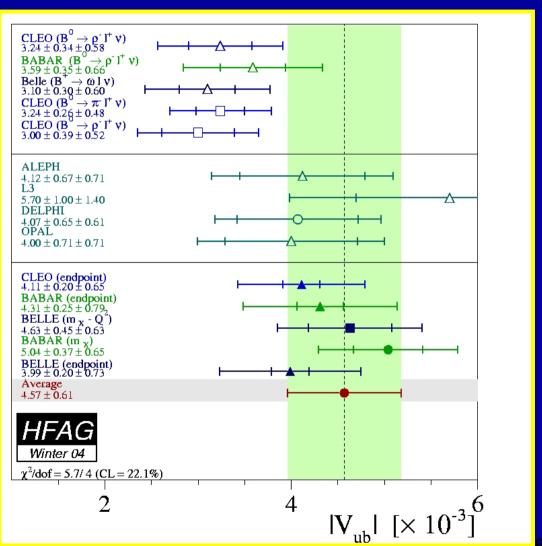


Exclusive/Inclusive Vub

Exclusive

Inclusive





Unitary Triangle Analysis: RESULTS AND PERSPECTIVES



Collaboration

M.Bona, M.Ciuchini, E.Franco, V.L., G.Martinelli,

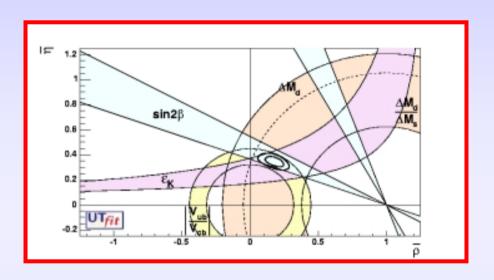
F.Parodi, M.Pierini, P.Roudeau, C.Schiavi,

L.Silvestrini, A.Stocchi

Roma, Genova, Torino, Orsay

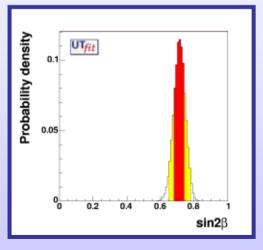
www.utfit.org

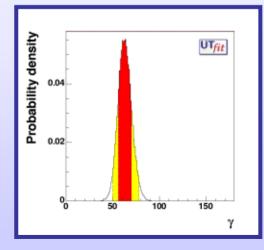
FIT RESULTS



$$\overline{\rho} = 0.174 \pm 0.048$$

$$\eta = 0.344 \pm 0.027$$





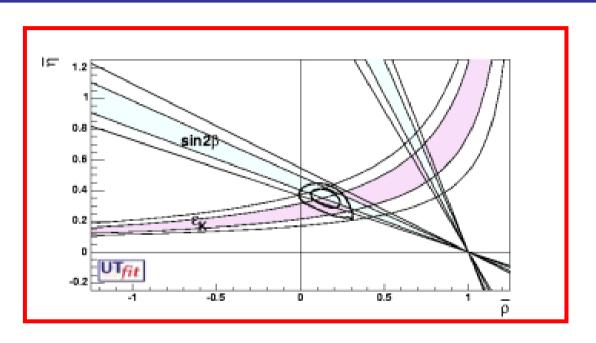
$$\sin 2\alpha = -0.14 \pm 0.25$$

$$Sin2\beta = 0.697 \pm 0.036$$

$$\gamma = (61.9 \pm 7.9)^{\circ}$$

INDIRECT EVIDENCE OF CP VIOLATION

3 FAMILIES → - Only 1 phase - Angles from Sides



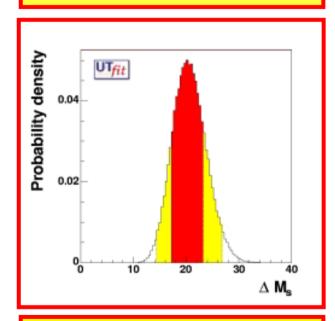
$$Sin2\beta_{UT \, Sides} = 0.685 \pm 0.047$$

 $Sin2\beta_{J/\psi Ks} = 0.739 \pm 0.048$

Prediction (Ciuchini et al., 2000): $\sin 2\beta_{\text{UTA}} = 0.698 \pm 0.066$ ₃₀

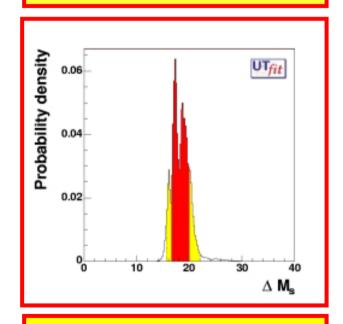
Prediction for Δm_s

∆m_s NOT USED



$$\Delta m_s = (20.5 \pm 3.2) \text{ ps}^{-1}$$

WITH ALL CONSTRAINTS



$$\Delta m_s = (18.0 \pm 1.6) \text{ ps}^{-1}$$

A measurement is expected at FERMILAB

IMPACT OF IMPROVED DETERMINATIONS

$$B_K = 0.86 \pm 0.06 \pm 0.14$$

$$\xi = 1.24 \pm 0.04 \pm 0.06$$

$$f_{Bs}\sqrt{B_{Bs}} = 276 \pm 38 \text{ MeV}$$

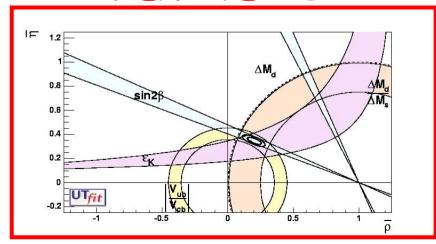
 $\sin 2\beta = 0.734 \pm 0.054$

$$V_{ub} = (32.4 \pm 2.4 \pm 4.6) 10^{-4}$$
 (exclusive only)

TODAY

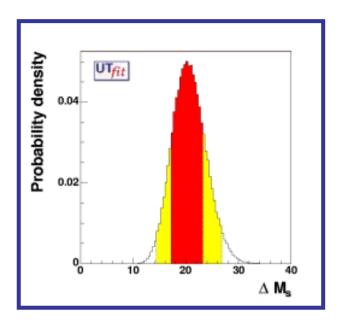
$$\Delta \overline{\rho} = 28\% \to 17\% (-40\%)$$

NEXT YEARS

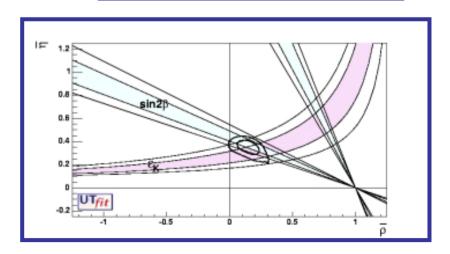


$$\Delta \overline{\eta} = 7.8\% \rightarrow 5.2\% (-33\%)$$

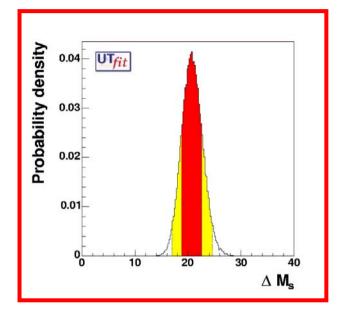
TODAY



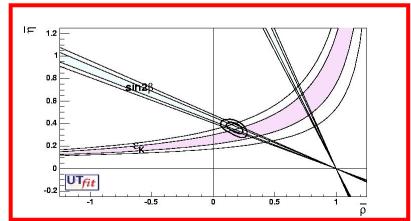
 $\Delta m_s = (20.5 \pm 3.2) \text{ ps}^{-1}$



NEXT YEARS



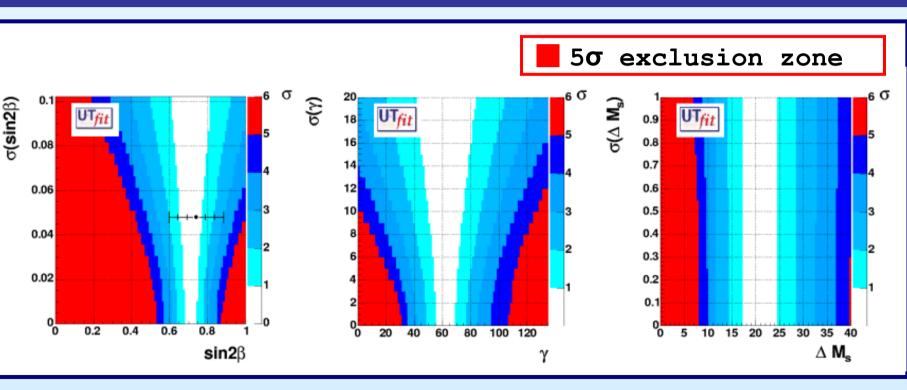
 $\Delta m_s = (20.7 \pm 1.9) \text{ ps}^{-1}$



NEW PHYSICS

THE "COMPATIBILITY" PLOTS

1) "To which extent improved experimental determinations will be able to detect New Physics?"



Compatibility between direct and indirect determinations as a function of the measured value and its experimental uncertainty

SEARCH FOR NEW PHYSICS

2) "Given the present theoretical and experimental constraints, to which extent the UTA can still be affected by New Physics contributions?"

An interesting case:

New Physics in B_d-B_d mixing

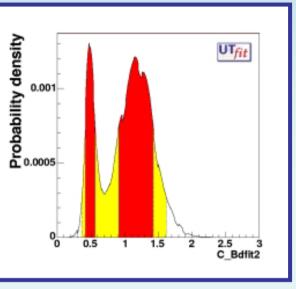
The New Physics mixing amplitudes can be parameterized in a simple general form:

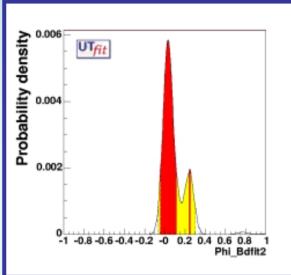
$$M_d = C_d e^{2i\varphi_d} (M_d)^{SM}$$

$$\Delta m_d = C_d (\Delta m_d)^{SM}$$

$$A(J/\psi K_S) \sim \sin 2(\beta + \phi_d)$$

TWO SOLUTIONS:



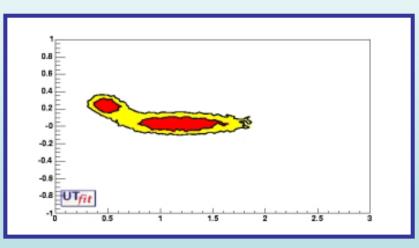


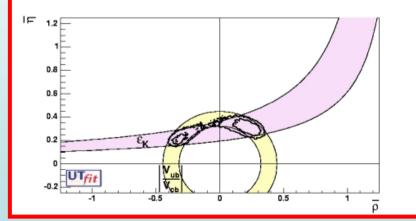
Standard Model solution:

$$C_d = 1 \ \phi_d = 0$$

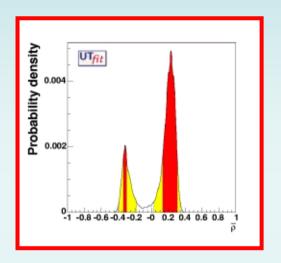
φ_d can be only determined up to a trivial twofold ambiguity:

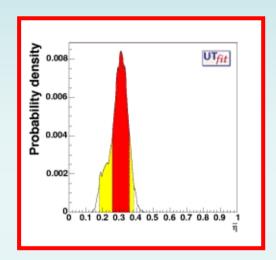
$$\beta\text{+}\phi_\text{d}\to\pi\text{-}\beta\text{-}\phi_\text{d}$$

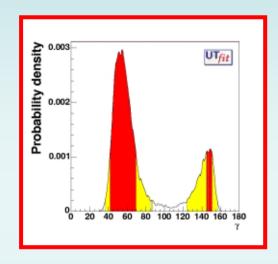




HOW CAN WE DISCRIMINATE BETWEEN THE TWO SOLUTIONS?







$$\Delta m_s$$
, η [$K_L \rightarrow \pi \nu \bar{\nu}$], γ [$B \rightarrow DK$], V_{td} [$B \rightarrow \rho \gamma$], ...

 $\gamma = 81^{\circ} \pm 19^{\circ} \pm 13^{\circ} \text{ (syst)} \pm 11^{\circ} \text{ (mod)}$

Belle

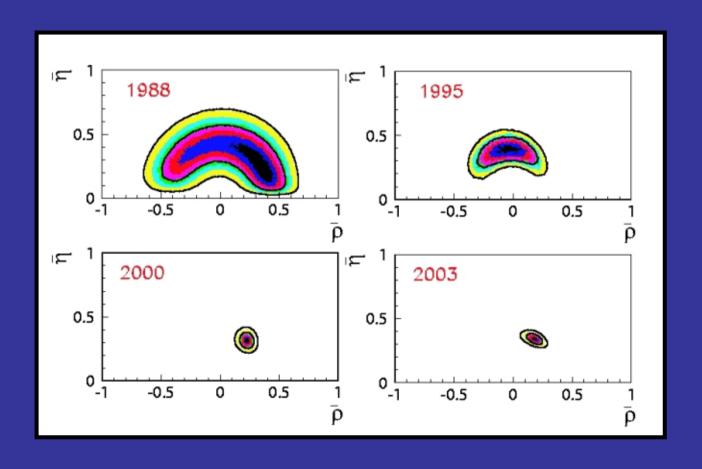
Independent of NP

Belle preliminary
+ LQCD(!)

Coming back to the Standard Model:

15 YEARS OF (p-η) DETERMINATIONS

(The "commercial" plot)



CONCLUSIONS

- LATTICE QCD CALCULATIONS HAD A CRUCIAL IMPACT ON TESTING AND CONSTRAINING THE FLAVOR SECTOR OF THE STANDARD MODEL
- IN THE PRECISION ERA OF FLAVOR PHYSICS, LATTICE SYSTEMATIC UNCERTAINTIES MUST (AND CAN) BE FURTHER REDUCED
- IMPORTANT, BUT MORE DIFFICULT PROBLEMS (NON LEPTONIC DECAYS, RARE DECAYS, ...) ARE ALSO BEING ADDRESSED